The interaction between waves and a turbulent current: waves propagating with the current

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This paper describes an experimental programme carried out in a laboratory channel with rough and smooth beds, to investigate the interaction between gravity waves and a turbulent current. In particular, changes induced in the mean-velocity profiles, turbulent fluctuations, bed shear stresses and wave attenuation rates are considered for a range of wave heights, keeping the wave period constant. The smooth-boundary tests were carried out as a necessary preliminary to the more-realistic rough-boundary condition.

A directionally sensitive laser anemometer was used to measure horizontal, vertical, and 45° velocity components in the oscillating fluid, and an on-line minicomputer was programmed to produce ensemble averages of velocities, Reynolds stresses and wave-elevation data. The cycle was sampled at 200 separate phase positions, with 180 observations at each position. Measurements were made at up to 30 points in the vertical.

Preliminary tests were carried out on the unidirectional current and on the waves alone. These show that mean-velocity profiles and turbulence parameters of the current agree satisfactorily with previous experiments, and that the waves are approximated closely by Stokes' second-order theory.

For combined wave and current tests, mean-velocity profiles are generally found to differ from those suggested by a linear superposition of wave and current velocities, a change in boundary-layer thickness being indicated. However, shear stresses at the smooth boundary are found to be described by such a linear addition.

1. Introduction

While considerable research has gone into the study of waves and currents separately, little is known about the way in which the combined flows interact, particularly close to the bed.

Grant & Madsen (1979) have produced a theoretical analysis of combined wave and current flow over a rough boundary, predicting an increase in apparent bed roughness and shear stress when waves are superimposed on the current. However, they stated that they require experimental data to validate these results. A similar theory has been presented by Christoffersen (1980), using a modified eddy-viscosity distribution. Bakker & van Doorn (1978) also found an increased apparent bed roughness for waves and currents combined. Changes in mean velocity profile have been measured by Brevik & Aas (1980) and by van Hoften & Karaki (1976), although measurements were not made close to the bed in either case. The results of Brevik & Aas indicate an



FIGURE 1. Diagram of channel layout and recirculating system.

overall reduction in mean velocity over depth when waves are superimposed on the current, although their outer flow measurements were not reliable.

George & Sleath (1979) measured the flow over an oscillated bed of spheres with a weak current superimposed, and described the cycle of vortex formation and ejection around the roughness elements. The stronger downstream vortex was found to induce a weak reverse mean current just above the roughness elements. This is consistent with the observations of Inman & Bowen (1963) and Bijker, Hijum & Vellinga (1976), who both reported enhanced upstream sediment transport when a weak current was superimposed on waves. The latter paper also observes that insight into the vortex formation as a function of wave and flow parameters is essential for an understanding of sand transport by waves and currents.

Over smooth boundaries, there is very little previous data on the wave-current interaction relevant to bed shear stress or turbulence intensities, although Binder & Favre-Martinet (1979) have reported a retardation in phase of wave-induced velocities near the bed when currents are imposed on a pulsed duct flow, contrary to the phase advance that occurs for waves alone.

The aim of the authors' research was to provide experimental data for the turbulentcurrent interaction with waves over both rough and smooth boundaries, and to observe any discrepancy between the measured mean- and turbulent-velocity distributions and those predicted by an assumption of linear superposition. Particular interest was paid to the near-boundary turbulent flow, with its implications for sediment motion.

2. Apparatus

The investigation was carried out in a specially constructed channel 14.5 m long, 457 mm wide and 690 mm deep, with provision for flow in either direction and wave generation by a bottom-hinged paddle at one end. Flow was supplied by a recirculating system with header tanks 16 m above. Inflow to the channel was controlled at a steel gate valve, while outflow was adjusted at three diaphragm valves – see figure 1.

Two bed conditions were used in the tests. The first was a smooth bed of gloss paint applied to the dural bed sections, and the second consisted of 5 mm high triangular wooden strips stuck across the channel width and spaced at 18 mm centres along the line



of flow. The latter was chosen so as to generate a rough turbulent boundary layer both with the unidirectional current, and also with the larger waves in the absence of a current. It was also of a similar geometric form to that used by Jonsson & Carlsen (1976) in their tests in an oscillating water tunnel.

3. Instrumentation and analysis

Fluid velocities were measured using a laser-Doppler anemometer, thus avoiding the introduction of a measuring probe into the reversing flow. Since a single-channel laser anemometer was used, average Reynolds stresses were determined from velocity measurements in two orthogonal directions at 45° to the horizontal (see appendix).

Analysis of turbulent and wave-induced velocities was carried out by an on-line PDP8E minicomputer. This was programmed to compute ensemble averages of the wave-induced velocity, the initial phases of which were synchronized by a 5V trigger pulse, actuated by the wave generator. The r.m.s. fluctuations \tilde{u}' about the ensemble averages \tilde{u} of the horizontal velocity component were also derived, \dagger and both time-and frequency-domain analysis was carried out on the turbulent fluctuations remaining

† Throughout this paper, for a quantity M, \widetilde{M} is the ensemble-average of M with \overline{M} subtracted (\overline{M} is the mean value over the full sample period):

$$\widetilde{M}(t) = N^{-1} \sum_{0}^{N-1} M(t+nT) - \overline{M}.$$

 \widetilde{M}' is the turbulence r.m.s. of M about periodic \widetilde{M} :

$$\widetilde{M}'(t) = \left\{ N^{-1} \sum_{0}^{N-1} M[(t+nT) - \widetilde{M}(t+nT) - \overline{M}]^2 \right\}^{\frac{1}{2}}.$$

	(i) Waves	alone;	T = 1.00)6 s			
	-	Smooth boundary			Rough boundary			
Wave height H (mm) Wavelength L (mm) Reflection coefficient	WA1 29·0 1210 6·0	WA3 37·8 1212 5·3	WA4 46·4 1216 5·4	WA5 54·4 1222 5·8	WR1 27·8 1210 3·4	WR3 36·8 1220 3·5	WR4 45·0 1208 3·9	WR5 48·7 1219 4·5
Depth of flow d (mm)	200			201				
	(ii) Waves with current; $T = 1$ Smooth boundary			006 s Rough boundary				
H (mm) L (mm) $\alpha_r (\%)$	WCA1 20·7 1426 10·4	WCA3 30·3 1425 9·9	WCA4 39·4 1430 8·6	WCA5 44·4 1433 8·6	WCR1 22·7 1457 8·8	WCR3 31·6 1457 7·8	WCR4 40·4 1467 7·4	WCR5 46·6 1475 7·2
d (mm) Mean centre-line velocity (current alone) u _B (mm/s)	200 183			201 185				
TABLE 1. V	Vave cha	racteristi	cs with a	and with	out curre	ent impos	sed	

after the ensemble averages had been removed from the full velocity signal. The computer also proved invaluable in constructing 'instantaneous' velocity profiles at phases through the wave cycle from sets of ensemble-average velocities.

Wave heights were found by ensemble-averaging the output of a resistance-type wave monitor, and wave period timed against the computer's real-time crystal clock.

4. Results for unidirectional current and wave alone

It was decided to keep the flow depth at the measuring section constant at 200 mm for all tests, and to use one overall flow rate through the channel. It was found that, to achieve this, only slight adjustments were necessary over the whole range of tests. Run CA was for unidirectional current over the smooth bed, run CR over the rough bed – see figure 2.

When scaled on suitable flow parameters, a logarithmic mean velocity profile was found to follow the universal law of the wall for both rough and smooth boundaries, with von Kármán's constants of 0.36 and 0.4 respectively. Average centre-line velocities $\overline{u}_{\rm B}$ were deduced from the measured profiles. Horizontal and vertical turbulence intensities, and Reynolds-stress measurements in the wall layer were in good agreement with previous research (Laufer 1950; Grass 1971).

Runs WA1-WA5 were for waves alone of increasing height over the smooth bed; WR1-WR5 were for waves over the rough bed. All waves tested were of 1 s period, and varied in height between 25 and 55 mm. This gives a range of $a_{\rm bm}/k_{\rm s}$ of 0.35-0.75, or $a_{\rm bm}/k_{\rm t}$ of 1.75-3.7. Here $a_{\rm bm}$ is the orbital amplitude of a particle at the outer edge of the wave boundary layer, $k_{\rm s}$ is the Nikuradse equivalent sand roughness, and $k_{\rm t}$ is the physical height of the triangular roughness elements. Reflection coefficients, derived

	WR1	WR3	WR4	WR5
H (mm)	27.8	36.8	45.0	48.8
$\frac{dH}{dx} \times 10^5$	82	116	138	136
$u_{\rm b}$ (mm/s)	72	95	114	133
$a_{ m bm}/k_{ m s}$	0.46	0.61	0.73	0.85
f_w	0.78	0.64	0.53	0.36
$f_{\rm w}$ (Jonsson)	1.21	0.86	0.68	0.57
$f_{\rm w}$ (Kajiura)	0.62	0.52	0.46	0.41

 $f_{\rm w}$ (Jonsson) calculated from $\frac{1}{4}f_{\rm w}^{-\frac{1}{2}} + \log_{10}\left(\frac{1}{4}f_{\rm w}^{-\frac{1}{2}}\right) = 0.20 + \log_{10}\left(a_{\rm bm}k_{\rm s}^{-1}\right);$

 $f_{\rm w}$ (Kajiura) calculated from $f_{\rm w} = 0.37 (a_{\rm bm}/k_{\rm s})^{-\frac{2}{3}}$.

 TABLE 2. Experimental and theoretical friction factors for waves over the rough boundary

by measuring wave heights at regular intervals less than a quarter of a wavelength apart, were of the order of 5% (see table 1).

Wave-surface profile and wave-induced periodic velocities corresponded to Stokes' second-order theory, except close to the smooth boundary, where Lamb's (1932) viscous oscillatory boundary-layer theory described the amplitude and phase shift of the velocities.

Turbulence intensity measured in the waves alone over the smooth bed was of the same low order as the electronic noise of the anemometer (< 5%). However, within 4 roughness heights of the rough bed, for all waves tested values were obtained far in excess of those measured in the turbulent unidirectional currents. Intensities varied considerably through the wave cycle, the greatest fluctuation being measured in the vertical component over the roughness trough. Maximum intensities over the roughness apex tended to occur simultaneously with minima over the trough. This was because of vortices forming and residing for most of the wave period in the trough, but being rapidly ejected over the apex each half-cycle.

The test programme included measurement of wave-height attenuation along the channel, from which the rough boundary friction factor $f_{\rm w}$ was determined, using equation (11) of Kamphuis (1978). This assumes first-order waves, and neglects side-friction. The results are set out in table 2, together with values derived from the turbulent oscillatory boundary-layer theories of Jonsson & Carlsen (1976) and Kajiura (1968). It should be pointed out that the waves under test had $a_{\rm bm}/k_{\rm s}$ values smaller than the ranges of validity of these two theories. Nevertheless, the experimental results lie between those predicted by the two theories.

5. Results – combined current and waves

Details of wave characteristics with and without current are given in table 1. Runs WCA1-WCA5 are of current superimposed on waves of increasing height over the smooth bed, and WCR1-WCR5 current and wave over the rough bed. Overall flow through the channel was as for the current alone, and the mean depth of flow at the



FIGURE 3. Wave profiles with and without current. (a) Rough-boundary runs WR3 and WCR3; (b) smooth-boundary runs WA4 and WCA4. ——, wave with current; - - -, wave alone.

measuring section was also maintained constant with only slight adjustment of outlet valves.

The wave-surface profile at the anemometer position was measured for each wave propagating on a current, by ensemble-averaging the output of the wave monitor. Comparison with theoretical profiles suggests that the addition of the current has had little effect on the close agreement between the measured waves and those of both second- and third-order theory. Figure 3 allows further comparison, by plotting equivalent profiles, scaled by wavelength and wave height, of the same waves with and without currents. It seems from this that there is a tendency for the currents to make the waves longer in the trough, and sharper crested, a result predicted by Dalrymple (1974). In addition, the presence of waves reflected from the beach is now more apparent, owing to their increase in wave height as they propagate against the



FIGURE 4. Normalized wave-induced velocities within 3 mm of the smooth bed; waves and current. $\beta = (\pi/\nu T)^{\frac{1}{2}}$ is the viscous-boundary wavenumber. Wave period T = 1 s, d = 200 mm, $\overline{u}_{\rm B} = 183$ mm/s. \odot , WCA1; +, WCA3; ×, WCA4; \blacktriangle , WCA5; --- Lamb's theory.

current. The height and phase of the reflected waves at the anemometer position have to be considered when interpreting wave-induced horizontal and vertical velocities \tilde{u} and \tilde{v} respectively.

A notable feature of the results from tests over both rough and smooth beds is the reduction in maxima and minima of the periodic wave-induced velocity \tilde{u} near the bed. This reduction is seen to extend further from the bed and to a greater degree in the steeper waves, the layer of reduced velocities extending 30 mm from the bed in run WCA5. Figure 4 contains normalized \tilde{u}_{max} and \tilde{u}_{min} very close to the smooth bed for all the waves on the current, together with the theoretical solution taken from Lamb (1932). It can be seen that there is good agreement, as for waves alone, with maximum amplitude reached at 1.4 mm from the bed level, despite the fact that there was now turbulence in the near-bed wave boundary layer.

5.1. Mean velocities

Mean velocities in the combined wave and current tests were obtained in the same way as for the waves alone, by averaging the anemometer signal over 180 wave cycles.

5.1.1. Full-depth profiles. These reveal that the main effects of introducing a wave and increasing the wave height H are to reduce the mean velocity in the upper layers and increase it in the turbulent boundary layer near the bed. It was decided to compare the combined wave-current experimental results with the linear addition of the separately measured unidirectional current and wave velocities. The wave velocities used were those for a wave of the same length and height as was measured at the anemometer position with the current flowing. Figure 5 shows these results together



FIGURE 5. Mean-velocity profiles over smooth bed: experimental and theoretical. (a) WCA1, H = 20.7 mm; (b) WCA3, 30.3 mm; (c) WCA4, 39.4 mm; (d) WCA5, 44.4 mm. $\times --- \times$, experimental results; $\bigcirc -- \bigcirc$, theoretical superposition of wave alone and current alone.

Sn	nooth-bound	lary tests			
	$\mathbf{C}\mathbf{A}$	WCA1	WCA3	WCA4	WCA5
Shear velocity \overline{u}_* (mm/s)	8.66	8.89	9 ·01	8.98	8.68
Bed shear stress $\tau_{\rm b}$ ($\times 10^{-3}$ Pa)	75.0	79 ·1	81.2	80.6	75.3
B^{\dagger}	10.2	10.3	10.8	11.3	11.9
Displacement thickness	15.4	10.7	7.1	5.5	4.5
$\delta_{\ast} \left(= \int_{0}^{\infty} \left(1 - \frac{\overline{u}}{\overline{u}_{\infty}} \right) dy \right) (\text{mm})$					
Momentum thickness	11.6	8.1	$5 \cdot 1$	4 ·0	3.3
$\theta\left(=\int_{0}^{\infty}\frac{\overline{u}}{\overline{u}_{\infty}}\left(1-\frac{\overline{u}}{\overline{u}_{\infty}}\right)dy\right)(\mathrm{mm})$					
Outer flow velocity \overline{u}_{∞} (mm/s)	205	196	191	188	182
Viscosity $\nu \ (mm^2/s)$	1.16	1.02	1.14	1.13	1.14
Reynolds number R_{θ} $(= \overline{u}_{\infty} \theta / \nu)$	2060	1550	860	670	520
† B calculated	from $\overline{u}/\overline{u}_*$:	$= (1/k) \ln ($	$y\overline{u}_{*}/\nu)+B.$		
R	ough-bound	ary tests			
	\mathbf{CR}	WCR1	WCR3	WCR4	WCR5
$\overline{u}_* \text{ (mm/sec)}$	14.7	18-1	19-3	20.1	18.7
$ au_{ m b}~(imes 10^{-3}~{ m Pa})$	215	328	372	405	350
Roughness length y_0 (mm)	0.835	1.25	1.29	1.67	1·86
Nikuradse roughness k_s (mm)	25	37	39	50	56
δ* (mm)	$25 \cdot 0$	21.3	$15 \cdot 1$	14.9	18.9
heta (mm)	15.3	13.4	9·1	8.8	11.3
$\overline{u}_{\infty} (\text{mm/s})$	219	221	211	198	189
$\nu (\mathrm{mm^2/s})$	1.087	0.986	0.986	0.998	1.035
$R_{ heta}$	3160	3000	1970	1790	2100
TABLE 3. Boundary-	layer param	neters: curr	ents with w	vaves	



FIGURE 6. Semi-logarithmic velocity profiles over smooth boundary: $\overline{u} vs$. log y. \Box , current alone CA. Wave and current: \bigcirc , WCA1; +, WCA3; ×, WCA4; \triangle , WCA5.



FIGURE 7. Variations in boundary-layer parameters and \overline{u}_{∞} with H. —— ∇ ——, rough-bed \overline{u}_{∞} ; —— Δ —, smooth-bed \overline{u}_{∞} ; \bigcirc — \cdot — \bigcirc , rough-bed δ_{*} ; \bigcirc — \cdot — \bigcirc , smooth-bed δ_{*} ; \diamondsuit — $--\diamondsuit$, smooth-bed δ_{*} ; \diamondsuit — $--\diamondsuit$, smooth-bed B.

with the experimental results, from which it can be seen that a simple law of superposition does not hold. Measured velocities are larger near the boundary and smaller in the outer flow than for the added component flows, with the latter trend becoming more pronounced in the highest wave. These results suggest that the boundary-layer thickness has been diminished by the addition of the waves, a finding reinforced by the reduction in displacement and momentum thickness calculated – see table 3.

Over the rough boundary, a somewhat different pattern emerges. In the outer flow



there is a noticable reduction in \overline{u} with increasing H, as for the smooth bed tests. But near the roughness elements at the bed, there is a more complex change. Within two roughness heights of the apex level there is a reduction in \overline{u} with increasing H, as found in the outer flow. However, a reduction was found in the boundary-layer thickness at the side walls from 30 to 5 mm when the largest wave WCR5 was imposed on the current, and it was also noted that the secondary flow cells had moved. From these findings it was concluded that a comparison of outer flow velocities would be influenced by the side walls. Thus, the main study of the changes in characteristics of the turbulent boundary layer has to be limited to the near-bed layer, less influenced by side-wall boundary layers.

5.1.2. Boundary-layer profiles. In the unidirectional-current tests, the logarithmic law of the wall was found to hold good over both rough and smooth beds. Over the smooth bed, the same is found when waves are superimposed – see figure 6. However, certain differences in the profiles are apparent. For the three smaller waves over the smooth boundary, the effect of increasing wave height is to give a uniform increase to the mean velocity through the logarithmic region. The largest wave, WCA5, produces no further increase in \bar{u} , however, and the curve drops off beyond the outer edge of the logarithmic layer. The mean-velocity profiles in the bottom 3 mm of flow for all tests with and without waves each exhibit parallel, linear regions indicating that the shear stress $\bar{\tau}_{\rm b}$ at the channel bed is unaffected by the oscillatory motion. It also seems, however, that the viscous stresses are effective further from the boundary as H increases, although the extent of the *linear* portion does not increase.

A common feature of all the rough boundary tests is that although they exhibit a logarithmic layer, the mean shear stress deduced from the slope of the logarithmic profile is significantly higher than that for the current alone. It is also seen (see table 3 and figure 7) that the roughness length scale y_0 (the intercept of the log line with





 $\overline{u} = 0$) increases with wave height up to two times the current-only value. However, the cross-channel redistribution of flow for the larger waves makes too close an analysis of the profiles questionable, and the evaluation of the mean of the shear velocity \overline{u}_* from the logarithmic region is sensitive to the number of measurements in the layer. $(u_* = \tau_b^{\frac{1}{2}} \rho^{-\frac{1}{2}})$, where ρ is density.)

Measurements over the trough of the bed roughness show that there is an increase in return (against the current) flow between the elements over that measured with the current alone. However, for run WCR4, the maximum negative \overline{u} is further from the trough level than with the two smaller waves, and in run WCR5, the largest wave,

Measurements in					
viscous layer	$\mathbf{C}\mathbf{A}$	WCA1	WCA3	WCA4	WCA5
$\overline{u}_* (\mathrm{mm/s})$	8.6	8.9	8.9	9.3	8.9
$\tilde{u}_{*\max}$	—	13.4	16.2	16.8	18.2
$\tilde{u}_{*\min}$		-3.7	- 7.8	- 9.1	-12.4
$ar{ au} imes 10^{-3} \mathrm{Pa}$	74	79	80	86	79
$ ilde{ au}_{ ext{max}}$		180	262	283	332
$ ilde{ au}_{ ext{min}}$	—	- 14	- 61	- 83	- 153
Measurements in logarithmic layer					
\overline{u}_{\pm}	8.7	8.9	9.0	9.0	8.7
$\tilde{u}_{\pm \max}$	_	9.9	9.8	10.3	10.4
$\overline{ au}$	75	79	81	81	75
${ ilde au}_{ ext{max}}$	—	98	97	107	108
Theoretical addition of wave and current velocities in the viscous layer					
ũ.	8.6	$14 \cdot 2$	16.0	17.7	18.5
τ _{mbx}	74	203	257	315	344
TABLE 4.	Mean and	periodic shea	r-stress paran	neters	

there is a reduction in the return flow. This decrease is a consequence of the increased part of the wave cycle during which flow above the bed is against the current. The duration of this reverse flow increases with H, thus allowing the formation of 'upstream' vortices, which induce downstream velocities in the roughness troughs. The extent of flow reversal is made more clear in ensemble-average velocity profiles such as those in figures 8 and 9.

It is of interest to note that flow reversal takes place near the smooth bed for all the waves tested, in the smallest, WCA1, within only 0.4 mm, but for the largest, WCA5, over 3 mm. Such reversal involves an inflection in the velocity profile, normally a sign of instability in steady flow. Over the rough bed the reversal layer is thicker, varying between 3 and 15 mm above apex level.

From the velocity profiles close to the smooth bed, it is possible to calculate the maximum and minimum bed shear stress, $\tilde{\tau}_{\max}$ and $\tilde{\tau}_{\min}$, induced periodically by the waves and currents. These are presented in table 4, with corresponding values of \tilde{u}_* . Also included are measurements of \tilde{u}_* derived from the slope of the logarithmic velocity profile. It is seen that the maximum bed shear velocity is approximately double the mean-over-the-wave-cycle estimate \bar{u}_* for the larger waves. It is also apparent that the large periodic variations in \tilde{u}_* close to the bed are not transmitted out into the logarithmic region, although the value of \tilde{u}_* was found to vary from \bar{u}_* in this layer by 20 % in the larger waves, and 10 % in the smaller. This indicates a wave-influenced turbulence, apparent from the maximum periodic velocities, \tilde{u}_{\max} , discussed in § 5.2, although no such turbulence was found in the tests on waves alone.

Graphs of velocity profiles at phases corresponding to the passage of wave crests and troughs through the measuring section over the rough bed reveal that the logarithmic slope again remains virtually constant through the wave cycle-see figure 10; and, when scaled on instantaneous shear velocity and y_0 , all the curves fall back onto the same



FIGURE 10. Semi-logarithmic velocity profiles over rough bed at phases corresponding to wave crest and wave trough (measured over roughness apex). $\times \cdots \times$, WCR1; $\bigtriangledown --- \bigtriangledown$; WCR3; $\Box --- \Box$, WCR4; $\bigcirc --- \diamondsuit$, WCR5.

line, as seen in figure 11, although the logarithmic portion occurs at differing y/\tilde{y}_0 for wave crests and troughs.

The phase of the horizontal periodic velocity component was also measured, relative to the wave-surface profile. It was found that the phase advance near the rough bed was slightly less than for the case of waves alone, but was still of the order of 25° .

5.2. Turbulence characteristics

5.2.1. Smooth boundary. It is found that the horizontal turbulence component varies through the wave cycle. Very close to the bed, in the layer where wave action induces flow reversal, there are peaks in r.m.s. at the phases corresponding to zero absolute velocity $\bar{u} + \tilde{u}$, the larger disturbance being during the decelerating part of the cycle.

The periodicity of \tilde{u}' in the logarithmic region can be explained as the action of the vertical oscillatory motion on the vertical distribution of \tilde{u}' . Phases of maximum horizontal velocity correspond to maximum vertical displacement away from the bed, such motion carrying fluid of higher turbulence intensity from below. Only at the two phases mentioned above do the intensities for the combined wave-current flow exceed those of the unidirectional current, and by less than 25 %. The same applies also to the



FIGURE 11. Normalized semi-logarithmic velocity profiles measured over rough-bed apex, at phases corresponding to wave crest and trough. Symbols as in figure 10.



FIGURE 12. \tilde{u}' vs. log y: smooth-bed tests with current. - -, current alone CA; u'. Wave and current; \tilde{u}'_{max} : \bigcirc , WCA1; +, WCA3; ×, WCA4; \triangle , WCA5.

logarithmic layer. However, further from the bed the combined flow intensities fall below the values for current alone as far as the edge of the boundary layer. This bears out the results of the mean-velocity profiles, that the addition of waves reduces the thickness of the boundary layer.

It appears that no greater increase in turbulence intensity is achieved with the



FIGURE 13. Reynolds-stress distribution over smooth bed. $\times ---\times$, current alone CA. Wave and current: $\bigcirc --\bigcirc$, WCA1; $\blacktriangle ---\bigstar$, WCA5.

addition of the wave, although the maximum value of \tilde{u}'_{max} , found in the region close to y = 1.5 mm, does increase by approximately 20 %. This is shown more clearly on a semi-logarithmic scale, in figure 12.

It is seen from figure 13 that the superposition of the waves causes a considerable reduction in the turbulence stress, both near the boundary and in the outer flow. The apparent reduction in $\widetilde{u'v'}$ near the bed without a corresponding reduction in $\widetilde{u'}$ and $\widetilde{v'}$ can be reconciled by the suggestion, made above, that the generation of the turbulence is to some extent periodic with the wave. This would result in a certain proportion of the turbulent-velocity fluctuations being absorbed into the ensemble-mean values. Any turbulent flow with a superimposed period motion will present similar difficulties in extracting true turbulence intensities and Reynolds stresses if part of the generation process is directional and periodic, such as the regular ejection of vortices from a rough boundary. Thus a fluctuation in the flow which is an integral part of the turbulence mechanism can contribute to the ensemble average and not appear as measured turbulence intensity.

5.2.2. Rough boundary. It is seen that turbulence intensity fluctuates considerably in both directions through the wave cycle, particularly within two roughness heights above the bed apex, a layer 10 mm thick. Here, there is a maximum intensity at a phase corresponding to maximum horizontal deceleration, with a small peak during the accelerating phase. These characteristics are shared by measurements over roughness trough and apex, and by \tilde{u}' and \tilde{v}' components – see figures 14 and 15.

The superposition of even the smallest wave tested causes a dramatic increase in turbulence over the values for current flow alone. To emphasize the increase of intensity with wave height, figure 16 contains profiles of \tilde{v}_{\max} for 25 mm above the roughness apex level, including the results from all the combined wave-current tests, together



FIGURE 14. \hat{v}' vs. phase angle ψ over rough-bed apex: run WCR4.

with the unidirectional current values. It is seen from figure 17 that these intensities, even when scaled on the increased wave and current shear velocity, do not fall back to the values for current alone.

Figure 18 reveals that the rate of increase with wave height of turbulence intensities near the boundary is reduced by the addition of the current, for the range of wave heights considered.

If the maximum u'v' during a cycle of the largest wave, WCR5, is extracted it is found to be up to three times the unidirectional current value in the layer 10 mm above



FIGURE 15. \tilde{u}' vs. phase angle ψ over rough-bed apex: run WCR4.

the roughness apex, but returns to the mean-over-cycle value further from the bed. A sharp dip in Reynolds stress $\widetilde{u'v'}$ 1 mm above the roughness apex for tests on waves alone, attributed to the ejection of the upstream vortex, is no longer distinct, whereas the peak $\widetilde{u'v'}$ at the phase of ejection of the downstream vortex, not particularly clear in the tests on waves alone, has now become the dominant feature, occupying a considerable part of the wave cycle.



FIGURE 16. v'; \hat{v}'_{max} vs. y within 25 mm of bed-roughness apex: waves with current. $\dot{\cdots}$, current alone; v'. Wave and current; \hat{v}'_{max} : \triangle , WCR1; +, WCR3; ×, WCR4; \triangle , WCR5. Measurements taken over a bed roughness element.



FIGURE 17. Normalized vertical turbulence intensity above bed-roughness apex. Symbols as in figure 16.

5.3. Discussion

From the foregoing presentation of combined wave-current results, it is immediately apparent that no law of linear superposition is likely to predict the new flow in every respect.



FIGURE 18. Increase of ϑ'_{max} with wave height. Wave and current: (a) + - + , 5 mm above trough; $(b) \times \cdots \times , 1 \text{ mm}$ above apex; $(c) \oslash \cdots \oslash , 20 \text{ mm}$ above apex. Wave alone: $(d) \bigtriangleup - - \bigtriangleup , 5 \text{ mm}$ above trough; $(e) \bigtriangledown - - - \bigtriangledown , 1 \text{ mm}$ above apex; $(f) \bigcirc - \cdots \bigcirc , 20 \text{ mm}$ above apex. Note: $\vartheta'_{max} = v'$ when H = 0.

An important aspect of research into waves superimposed on turbulent currents is the effect that such a flow might have on sediment motion. In table 4, it was shown that the maximum smooth bed shear stress during a wave cycle is considerably increased over both the value in unidirectional flow and that found by averaging over a full cycle. If one compares these measured maximum stresses with theoretical values derived assuming a linear superposition between the current and waves of the same height, they are seen to be of the same order, generally within 10 % of the predicted values.

Thus a linear law of superposition does appear appropriate as a guide to the maximum shear periodically experienced. However, the use of such a simple model to predict the pick-up of sediment from the bed is complicated by the cyclic nature of the turbulence intensities in the near-bed layer. At the phase of maximum bed shear, the turbulence is at its lowest value and it is only during the decelerating, adverse-pressure phase that enhanced turbulence is present to increase diffusion of the sediment from the bed. Nor would a linear model predict the limit imposed on the diffusion by the contraction of the boundary layer.

The results shown in figure 7 indicate that the addition of waves of increasing height to a current over a rough boundary increases the apparent roughness by up to a factor of 2 and reduces the outer flow velocity. These trends are both predicted by Grant & Madsen (1979) and by Christoffersen (1980). For the present tests, using the Grant & Madsen approach, the expected increase in bed roughness should have been up to 70 $%_0$,



FIGURE 19. Eddy-viscosity distribution over rough bed: run WCR3. ..., Christoffersen (1980); ---, Grant & Madsen (1979); —, present data. $\epsilon = \overline{\tau}_{\rm b} (\rho d\overline{u}/dy)^{-1}$ for wave and current.

while they suggest a reduction in mean-over-depth velocity $\overline{u}_{\rm B}$ of 33 %. The experimental results of Brevik & Aas (1980) and Bakker & van Doorn (1978) both also show a considerable drop in $\overline{u}_{\rm B}$ with the addition of waves to a current. However, neither explain how the current can be considered to be the same when there appears to be less flow along the channel when waves are added. In the tests reported here, the average bed shear stress over the rough bed increases with wave height (see table 3), but this is associated with a systematic decrease in boundary-layer thickness at both the bed and the side walls. The net effect on overall discharge is small.

With the finite-height waves used in the present investigation the orbital velocities attenuate significantly below the water surface. As a result, the velocities measured at a given fixed point in the flow throughout a wave cycle are associated with different orbits, having different diameters. As Jonsson (1978) pointed out, there is a net forward transport of fluid over a wave period between trough and crest. This effect is reversed below trough level owing to orbit attenuation. To remove this effect from the measurements in order to arrive at the mean unidirectional current velocity superposed on the waves, the measured velocities were adjusted using second-order wave theory.

The bed shear stress for the largest wave tested showed a change in trend from the other waves, suggesting that a new flow regime may be developing as the orbital amplitude at the bed increases in relation to the spacing of the bed roughness.

In figures 10 and 11, it was shown that the logarithmic profile is still descriptive of a combined wave-current flow field, even through the wave cycle. This lends credibility to the various theories for combined waves and currents which are based on the assumption of a logarithmic layer.

Grant & Madsen assume a boundary layer of two regions with a linearly varying eddy viscosity in each. Figure 19 suggests that this is reasonable for most of the outer layer, although in the wave layer near the bed the distribution is scattered, and suggests a constant value of eddy viscosity.

The extent of the wave boundary layer δ_{w} , in the combined flow field, can be assessed either from turbulence data (figure 16) where intensities fall back to a constant value away from the bed, or from ensemble-average velocity profiles (figure 9). Both indicate $7.5 < \delta_w < 10.00 \text{ mm}$ for all waves tested, giving a ratio of δ_w/k_s of 0.4. This compares with 0.27 calculated from equation (50) of Christoffersen (1980).

The near-bed response of the flow over the rough boundary to the waves is generally different from that over the smooth bed, with both mean velocity and turbulence dependent on boundary geometry. The two positions selected for measurement of vertical profiles do not give a full picture of the flow structure in the region, in particular the size of the vortices at various phases of the wave. However, they do succeed in showing up the contrasting features of flow over a roughness apex and in a trough.

The present study bears out the considerable dominance of the downstream vortex in the turbulent characteristics of the layer, with a resulting decrease in mean velocity near the bed. It also confirms the findings of Bijker *et al.* (1976) that the addition of a current to an oscillatory motion may increase upstream sediment transport.

The relatively large physical size of the bed roughnesses compared with the laser measuring volume means that the definition of turbulence near the bed is not clear. This is because turbulence-generating vortices are periodic in this layer, and accordingly appear not in the turbulence r.m.s. component, but in the ensemble average.

6. Conclusions

(1) The unidirectional turbulent boundary layer is reduced in thickness by the superposition of waves propagating with the current over both rough and smooth beds. Side-wall boundary layers are also reduced, leading to a redistribution of flow across the channel.

(2) For all combined wave and current tests, flow reversal was experienced near the bed.

(3) Mean velocities near the smooth bed are increased by the addition of waves, whereas near the rough bed they are reduced. The latter is due to a change in the vortex pattern formed between bed roughness elements.

(4) The logarithmic portion of the mean velocity profiles over the rough boundary indicates an increase in mean bed shear stress $\bar{\tau}$ and roughness length scale y_0 with wave height. For the larger waves tested, $\bar{\tau}$ and y_0 are approximately double their values for current alone.

(5) Over the smooth boundary, maximum horizontal turbulence intensity during the cycle, for combined wave and current tests, is 20 % higher than for the current alone. Within 20 mm of the bed turbulence intensity is periodic, of amplitude up to 10 %.

(6) Within 2 roughness heights of the rough bed, the turbulence characteristics are dominated by the periodic formation of vortices at the bed. Maximum turbulence intensities and Reynolds stresses measured in the combined flow are up to three times their values for current alone, and they vary by over 50 % about their mean values during a wave cycle.

(7) For the range of waves tested, turbulence parameters near the rough boundary increase more rapidly with wave height for tests on waves alone than for waves propagating on a following current.

7. Possible implications in relation to sediment transport

The entrainment of sediment under flat-bed conditions can be related to the predicted instantaneous shear stress. However, although the entrainment of material from the bed can be considered to show a considerable increase under the combined action of waves and currents, the distribution of turbulence intensities suggests that the zone of diffusion would not increase. In fact, the results indicate a reduction in boundary-layer thickness. One might expect, therefore, that there would be an increase in sediment concentration in the near-bed region. In the light of Nielsen's (1979) observations, this distribution would change dramatically under spilling breakers, the material rapidly dispersing over the whole depth of flow.

The greater turbulent stresses found when waves are superimposed on a current are likely to result in a considerable increase in sediment pickup from a rippled bed. While the increase in turbulence is limited to a region within 6 or 7 roughness heights of the bed with a tendency for this zone to decrease with wave height for a constant wave period, it is to be expected that sediment brought into suspension by the near-bed vortex action will be diffused over the zone of the current-induced turbulence. This could result in significantly higher transport rates as long as the increased bed shear stress is not such as to prevent the formation of high bed ripples.

In the case of waves alone, the shear stresses at the bed are of the same order as for combined wave and current flow, but the vortex-dominated layer extends only approximately four roughness heights above the bed, and the only means of transporting sediment is by relatively weak wave-induced mean velocities. The limited thickness of the wave-induced vortex layer over a rippled bed has previously been noted by Tunstall & Inman (1975). This suggests that sediment would be concentrated in this near-bed layer.

8. Continuing research

The test-channel and experimental techniques described herein are at present being used in a study of flows in which waves and current propagate in opposite directions. The periodic nature of the near-boundary turbulence, wave attenuation and boundarylayer thickness are of particular interest. It is also intended to introduce sediment into the flow to observe the actual effects of the flow interaction on transport rates.

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Appendix

τ from Reynolds-stress measurements

Without the use of a two-channel anemometer, it is necessary to combine two sets of measurements at 45° to the horizontal, each of which is related to the uv correlation, to obtain average and ensemble-average Reynolds stresses. If \overline{A} , \overline{B} are the 45° mean-

velocity components and a', b' the turbulence fluctuations, then these are related to the horizontal \overline{U} , u' and vertical \overline{V} , v' components by

$$\bar{A} + a' = (\bar{U} + u')\cos 45^\circ + (\bar{V} + v')\sin 45^\circ, \tag{1}$$

$$\bar{B} + b' = (\bar{U} + u')\cos 45^\circ + (\bar{V} + v')\sin 45^\circ.$$
⁽²⁾

Taking the mean values, and squaring, combining (1) and (2):

$$\bar{A}^2 - \bar{B}^2 = \frac{1}{2}(\bar{U} + \bar{V})^2 - \frac{1}{2}(\bar{U} - \bar{V})^2 = 2\bar{U}\bar{V}.$$
(3)

Conversely, squaring first, then taking mean values:

$$(\overline{A} + a')^{2} - \overline{(\overline{B} + b')^{2}} = \frac{1}{2} [\overline{(\overline{U} + u' + \overline{V} + v')^{2} - (\overline{U} + u' - \overline{V} - v')^{2}}]$$

$$= 2 [\overline{(\overline{U} \cdot \overline{V} + \overline{U} \cdot v' + u' \cdot \overline{V} + u'v')}],$$

$$\overline{A}^{2} + \overline{B}^{2} + \overline{a}'^{2} - \overline{b}'^{2} = 2 \overline{U} \cdot \overline{V} + 2u'v'.$$
(4)

or

Combining (3) and (4):

Hence, Reynolds stress

$$\overline{a'^{2}} - \overline{b'^{2}} = \overline{2u'v'}$$

$$\overline{u'v'} = \frac{1}{2}(\overline{a'^{2}} - \overline{b'^{2}}).$$
(5)

or

$$\rho \overline{u'v'} = \frac{1}{2}\rho (\overline{a'^2} - \overline{b'^2}). \tag{6}$$

Equation (6) is used to calculate Reynolds stresses $\rho u'v'$ through the depth of flow, and $\rho u'v'$ through the wave cycle.

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